

# Solutions to Self-Test Problems

# CHAPTER 2

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ST-1
         a. EBIT
                                $5,000,000
             Interest
                                1,000,000
             EBT
                                $4,000,000
             Taxes (40%)
                                 1,600,000
                                $2,400,000
             Net income
         b.
                                     NCF = NI + DEP and AMORT
                                          = $2,400,000 + $1,000,000 = $3,400,000
         c.
                                  NOPAT = EBIT(1 - T)
                                          = $5,000,000(0.6)
                                          = $3,000,000
         d.
                                  NOWC = Operating current assets – Operating current liabilities
                                          = (Cash + Accounts receivable + Inventory)
                                            - (Accounts payable + Accruals)
                                          = $14,000,000 - $4,000,000
                                          = $10,000,000
                Total net operating capital = NOWC + Operating long-term assets
                                          = $10,000,000 + $15,000,000
                                          = $25,000,000
                                     FCF = NOPAT - Net investment in operating capital
         e.
                                          = \$3,000,000 - (\$25,000,000 - \$24,000,000)
                                          = $2,000,000
         f.
                                     EVA = EBIT(1 - T) - (Total capital)(After-tax cost of capital)
                                          = \$5,000,000(0.6) - (\$25,000,000)(0.10)
                                          = \$3,000,000 - \$2,500,000 = \$500,000
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ST-1 Argent paid \$2 in dividends and retained \$2 per share. Since total retained earnings rose by \$12 million, there must be 6 million shares outstanding. With a book value of \$40 per share, total common equity must be \$40(6 million) = \$240 million. Since Argent has \$120 million of debt, its debt ratio must be 33.3%:

$$\frac{\text{Debt}}{\text{Assets}} = \frac{\text{Debt}}{\text{Debt} + \text{Equity}} = \frac{\$120 \text{ million}}{\$120 \text{ million} + \$240 \text{ million}}$$
$$= 0.333 = 33.3\%$$

ST-2 a. In answering questions such as this, always begin by writing down the relevant definitional equations and then start filling in numbers. Note that the extra zeros indicating millions have been deleted in the calculations below.

(1) 
$$DSO = \frac{Accounts \ receivable}{Sales/365}$$
 
$$40.55 = \frac{AR}{Sales/365}$$
 
$$AR = 40.55(\$2.7397) = \$111.1 \ million$$

(2) 
$$\text{Quick ratio} = \frac{\text{Current assets - Inventories}}{\text{Current liabilities}} = 2.0$$
 
$$= \frac{\text{Cash and marketable securities} + \text{AR}}{\text{Current liabilities}} = 2.0$$
 
$$2.0 = \frac{\$100.0 + \$111.1}{\text{Current liabilities}}$$
 
$$\text{Current liabilities} = (\$100.0 + \$111.1)/2 = \$105.5 \text{ million}$$

(3) Current ratio = 
$$\frac{\text{Current assets}}{\text{Current liabilities}} = 3.0$$

$$= \frac{\text{Current assets}}{\$105.5} = 3.0$$

Current assets = 3.0(\$105.5) = \$316.50 million

(4) Total assets = Current assets + Fixed assets = 
$$\$316.5 + \$283.5 = \$600$$
 million

(5) ROA = Profit margin × Total assets turnover 
$$= \frac{\text{Net income}}{\text{Sales}} \times \frac{\text{Sales}}{\text{Total assets}}$$
$$= \frac{\$50}{\$1,000} \times \frac{\$1,000}{\$600}$$
$$= 0.05 \times 1.667 = 0.083333 = 8.3333\%$$

(6) 
$$ROE = ROA \times \frac{Assets}{Equity}$$

$$12.0\% = 8.3333\% \times \frac{$600}{Equity}$$

$$Equity = \frac{(8.3333\%)($600)}{12.0\%}$$

$$= $416.67 \text{ million}$$

(7) Total assets = Total claims = \$600 million Current liabilities + Long-term debt + Equity = \$600 million 
$$$105.5 + Long-term debt + $416.67 = $600 million \\ Long-term debt = $600 - $105.5 - $416.67 = $77.83 million$$

*Note:* We could also have found equity as follows:

ROE = 
$$\frac{\text{Net income}}{\text{Equity}}$$
  
 $12.0\% = \frac{\$50}{\text{Equity}}$   
Equity =  $\$50/0.12$   
=  $\$416.67$  million

Then we could have gone on to find long-term debt.

b. Jacobus's average sales per day were 1,000/365 = 2.7397 million. Its DSO was 40.55, so accounts receivable equal 40.55(\$2.7397) = \$111.1 million. Its new DSO of 30.4 would cause AR = 30.4(\$2.7397) = \$83.3 million. The reduction in receivables would be \$111.1 - \$83.3 = \$27.8 million, which would equal the amount of cash generated.

(1) New equity = Old equity - Stock bought back  
= 
$$$416.7 - $27.8$$
  
=  $$388.9$  million

Thus,
$$New ROE = \frac{Net income}{New equity}$$

$$= \frac{\$50}{\$388.9}$$

$$= 12.86\% (versus old ROE of 12.0\%)$$

(2) New ROA = 
$$\frac{\text{Net income}}{\text{Total assets - Reduction in AR}}$$

$$= \frac{\$50}{\$600 - \$27.8}$$

$$= 8.74\% \text{ (versus old ROA of } 8.33\% \text{)}$$

New total assets = Old total assets - Reduction in AR   
= 
$$$600 - $27.8$$
   
=  $$572.2$  million

$$\frac{Debt}{Old\ total\ assets} = \frac{\$183.3}{\$600} = 30.6\%$$

while

$$\frac{\text{New debt}}{\text{New total assets}} = \frac{\$183.3}{\$572.2} = 32.0\%$$

# CHAPTER 4

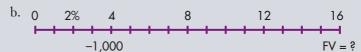
#### ST-1



\$1,000 is being compounded for 3 years, so your balance at Year 4 is \$1,259.71:

$$FV_N = PV(1+I)^N = \$1,000(1+0.08)^3 = \$1,259.71$$

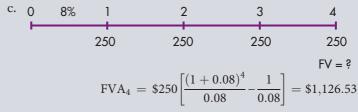
Alternatively, using a financial calculator, input N=3, I/YR = 8, PV =-1000, and PMT = 0; then solve for FV = \$1,259.71.



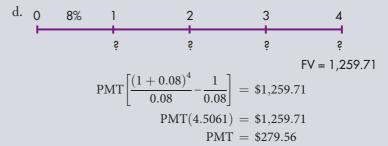
There are 12 compounding periods from Quarter 4 to Quarter 16.

$$FV_N = PV \left(1 + \frac{I_{NOM}}{M}\right)^{NM} = FV_{12} = \$1,000(1.02)^{12} = \$1,268.24$$

Alternatively, using a financial calculator, input N = 12, L/YR = 2, PV = -1000, and PMT = 0; then solve for FV = \$1,268.24.

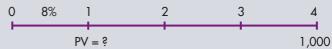


Using a financial calculator, input N=4, I/YR=8, PV=0, and PMT=-250; then solve for FV=\$1,126.53.



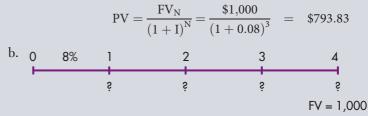
Using a financial calculator, input N = 4, I/YR = 8, PV = 0, and FV =1259.71; then solve for PMT = -\$279.56.

ST-2 a. Set up a time line like the one in the preceding problem:



Note that your deposit will grow for 3 years at 8%. The deposit at Year 1 is the PV, and the FV is \$1,000. Here is the solution:

$$N=3, \quad I/YR=8, \quad PMT=0, \quad FV=1000; \quad then \ PV=\$793.83.$$
 Alternatively,



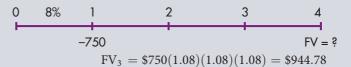
Here we are dealing with a 4-year annuity whose first payment occurs 1 year from today and whose future value must equal \$1,000. Here is the solution: N = 4; I/YR = 8; PV = 0; FV = 1000; then PMT = 1000\$221.92. Alternatively,

$$PMT \left[ \frac{(1+0.08)^4}{0.08} - \frac{1}{0.08} \right] = \$1,000$$

$$PMT(4.5061) = \$1,000$$

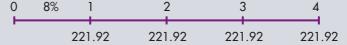
$$PMT = \$222.92$$

c. This problem can be approached in several ways. Perhaps the simplest is to ask this question: "If I received \$750 1 year from now and deposited it to earn 8%, would I have the required \$1,000 4 years from now?" The answer is "no":



This indicates that you should let your father make the payments rather than accept the lump sum of \$750.

You could also compare the \$750 with the PV of the payments:

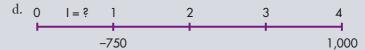


N = 4, I/YR = 8, PMT = -221.92, FV = 0; then PV = \$735.03.

Alternatively,

$$PVA_4 = \$221.92 \left[ \frac{1}{0.08} - \frac{1}{(0.08)(1+0.08)^4} \right] = \$735.03$$

This is less than the \$750 lump sum offer, so your initial reaction might be to accept the lump sum of \$750. However, it would be a mistake to do so. The problem is that, when you found the \$735.03 PVof the annuity, you were finding the value of the annuity today. You were comparing \$735.03 today with the lump sum of \$750 in 1 year. This is, of course, invalid. What you should have done was take the \$735.03, recognize that this is the PV of an annuity as of today, multiply \$735.03 by 1.08 to get \$793.83, and compare this \$793.83 with the lump sum of \$750. You would then take your father's offer to make the payments rather than take the lump sum 1 year from now.



N = 3, PV = -750, PMT = 0, FV = 1000; then I/YR = 10.0642%.

$$N = 4$$
,  $PV = 0$ ,  $PMT = -186.29$ ,  $FV = 1000$ ; then  $I/YR = 19.9997\%$ .

You might be able to find a borrower willing to offer you a 20% interest rate, but there would be some risk involved—he or she might not actually pay you your \$1,000!



Find the future value of the original \$400 deposit:

$$FV_6 = PV(1+I)^6 = 400(1+0.04)^6 = $400(1.2653) = $506.12.$$

This means that, at Year 4, you need an additional sum of \$493.88: \$1,000.00 - \$506.12 = \$493.88. This amount will be accumulated by making 6 equal payments that earn 8% compounded semiannually, or 4% each 6 months: N = 6, I/YR = 4, PV = 0, FV = 493.88; then PMT = \$74.46. Alternatively,

$$PMT \left[ \frac{(1+0.04)^6}{0.04} - \frac{1}{0.04} \right] = \$493.88$$

$$PMT(6.6330) = \$493.88$$

$$PMT = \$74.46$$
g.
$$EFF\% = \left( 1 + \frac{I_{NOM}}{M} \right)^M - 1.0$$

$$= \left( 1 + \frac{0.08}{2} \right)^2 - 1.0$$

$$= 1.0816 - 1 = 0.0816 - 8.16\%$$

ST-3 Bank A's effective annual rate is 8.24%:

EFF% = 
$$\left(1 + \frac{0.08}{4}\right)^4 - 1.0$$
  
=  $1.0824 - 1 = 0.0824 = 8.24\%$ 

Now Bank B must have the same effective annual rate:

$$\left(1 + \frac{I}{12}\right)^{12} - 1.0 = 0.0824$$

$$\left(1 + \frac{I}{12}\right)^{12} = 1.0824$$

$$1 + \frac{I}{12} = (1.0824)^{1/12}$$

$$1 + \frac{I}{12} = 1.00662$$

$$\frac{I}{12} = 0.00662$$

$$I = 0.07944 = 7.94\%$$

Thus, the two banks have different quoted rates—Bank A's quoted rate is 8%, whereas Bank B's quoted rate is 7.94%—yet both banks have the same effective annual rate of 8.24%. The difference in their quoted rates is due to the difference in compounding frequency.

# CHAPTER 5

ST-1 a. Pennington's bonds were sold at par; therefore, the original YTM equaled the coupon rate of 12%.

$$\begin{split} V_B &= \sum_{t=1}^{50} \frac{\$120/2}{\left(1 + \frac{0.10}{2}\right)^t} + \frac{\$1,000}{\left(1 + \frac{1.10}{2}\right)^{50}} \\ &= \$60 \left[ \frac{1}{0.05} - \frac{1}{0.05(1 + 0.05)^{50}} \right] + \frac{\$1,000}{\left(1 + 0.05\right)^{50}} \\ &= \$1,182.56 \end{split}$$

Alternatively, with a financial calculator, input the following: N = 50, I/YR = 5, PMT = 60, and FV = 1000; solve for PV = -\$1,182.56.

c. Current yield = Annual coupon payment 
$$\div$$
 Price 
$$= \$120/\$1,182.56$$

$$= 0.1015 = 10.15\%$$
Capital gains yield = Total yield - Current yield 
$$= 10\% - 10.15\% = -0.15\%$$
Total yield = Current yield + Capital gains yield 
$$= 10.15\% + (-0.15\%) = 10.00\%$$

 $$916.42 = \sum_{t=1}^{13} \frac{\$60}{(1+r_d/2)^t} + \frac{\$1000}{(1+r_d/2)^{13}}$ d.

With a financial calculator, input the following: N = 13, PV = -916.42, PMT = 60, and FV = 1000; then solve for =  $I/YR = r_d/2 = 7.00\%$ . Therefore,  $r_d = 14.00\%$ .

Current yield = 
$$120/$916.42 = 13.09\%$$
  
Capital gains yield =  $14\%-13.09\% = 0.91\%$   
Total yield =  $14.00\%$ 

e. The following time line illustrates the years to maturity of the bond:

Thus, on March 1, 2010, there were 13<sup>2</sup>/<sub>3</sub> periods left before the bond matured. Bond traders actually use the following procedure to determine the price of the bond.

(1) Find the price of the bond immediately after the next coupon is paid on June 30, 2010:

$$V_B = \$60 \left[ \frac{1}{0.0775} - \frac{1}{0.0775(1 + 0.0775)^{13}} \right] + \frac{\$1,000}{(1 + 0.0775)^{13}}$$
$$= \$859.76$$

Using a financial calculator, input N = 13, I/YR = 7.75, PMT = 60, and FV = 1000; then solve for PV = -\$859.76.

- (2) Add the coupon, \$60, to the bond price to get the total value, TV, of the bond on the next interest payment date: TV = \$859.76 +\$60.00 = \$919.76.
- (3) Discount this total value back to the purchase date:

Value at purchase date (March 1, 2010) = 
$$\frac{\$919.76}{(1 + 0.0775)^{(4/6)}}$$
$$= \$875.11$$

Using a financial calculator, input N = 4/6, I/YR = 7.75, PMT = 0, and FV = 919.76; then solve for PV = \$875.11.

(4) Therefore, you would have written a check for \$875.11 to complete the transaction. Of this amount,  $$20 = (\frac{1}{3})($60)$  would represent

- accrued interest and \$855.11 would represent the bond's basic value. This breakdown would affect both your taxes and those of the seller.
- (5) This problem could be solved *very* easily using a spreadsheet or a financial calculator with a bond valuation function.

ST-1 a. The average rate of return for each stock is calculated simply by averaging the returns over the 5-year period. The average return for Stock A is

$$r_{Avg A} = (-18\% + 44\% - 22\% + 22\% + 34\%)/5$$
  
= 12%

The realized rate of return on a portfolio made up of Stock A and Stock B would be calculated by finding the average return in each year as

$$r_A(\% \text{ of Stock } A) + r_B(\% \text{ of Stock } B)$$

and then averaging these annual returns:

Year	Portfolio AB's Return, r <sub>AB</sub>
2006	-21%
2007	34
2008	-13
2009	15
2010	<u>45</u>
	$r_{\text{Avg}} = \overline{\underline{12}}\%$

b. The standard deviation of returns is estimated as follows:

Estimated 
$$\sigma = S = \sqrt{\frac{\displaystyle\sum_{t=1}^{N} (\tilde{r}_t - \tilde{r}_{Avg})^2}{N-1}}$$

For Stock A, the estimated  $\sigma$  is about 30%:

$$\sigma_{A} = \sqrt{\frac{\left(-0.18 - 0.12\right)^{2} + \left(0.44 - 0.12\right)^{2} + \left(-0.22 - 0.12\right)^{2} + }{\left(0.22 - 0.12\right)^{2} + \left(0.34 - 0.12\right)^{2}}}$$

$$= 0.30265 \approx 30\%$$

The standard deviations of returns for Stock B and for the portfolio are similarly determined, and they are as follows:

	Stock A	Stock B	Portfolio AB
Standard deviation	30%	30%	29%

- c. Because the risk reduction from diversification is small ( $\sigma_{AB}$  falls only from 30% to 29%), the most likely value of the correlation coefficient is 0.8. If the correlation coefficient were -0.8, then the risk reduction would be much larger. In fact, the correlation coefficient between Stocks A and B is 0.8.
- d. If more randomly selected stocks were added to a portfolio,  $\sigma_P$  would decline to somewhere in the vicinity of 20%. The value of  $\sigma_P$  would remain constant only if the correlation coefficient were +1.0, which is most unlikely. The value of  $\sigma_P$  would decline to zero only if (1) the correlation coefficient  $\rho$  were equal to zero and a large number of

stocks were added to the portfolio or (2) the proper proportions were held in a two-stock portfolio with  $\rho = -1.0$ .

$$\begin{array}{lll} \text{ST-2} & a. & b = (0.6)(0.70) + (0.25)(0.90) + (0.1)(1.30) + (0.05)(1.50) \\ & = 0.42 + 0.225 + 0.13 + 0.075 = 0.85 \\ b. & r_{RF} = 6\%; \ RP_M = 5\%; \ b = 0.85 \\ & r_p = 6\% + (5\%)(0.85) \\ & = 10.25\% \\ c. & b_N = (0.5)(0.70) + (0.25)(0.90) + (0.1)(1.30) + (0.15)(1.50) \\ & = 0.35 + 0.225 + 0.13 + 0.225 \\ & = 0.93 \\ & r = 6\% + (5\%)(0.93) \\ & = 10.65\% \end{array}$$

# CHAPTER 7

ST-1 The first step is to solve for g, the unknown variable, in the constant growth equation. Since  $D_1$  is unknown but  $D_0$  is known, substitute  $D_0(1 + g)$  as follows:

$$\hat{P}_0 = P_0 = \frac{D_1}{r_s - g} = \frac{D_0(1+g)}{r_s - g}$$

$$\$36 = \frac{\$2.40(1+g)}{0.12 - g}.$$

Solving for g, we find the growth rate to be 5%:

$$$4.32 - $36g = $2.40 + $2.40g$$
  
 $$38.4g = $1.92$   
 $g = 0.05 = 5\%$ 

The next step is to use the growth rate to project the stock price 5 years hence:

$$\hat{P}_5 = \frac{D_0 (1+g)^6}{r_s - g}$$

$$= \frac{\$2.40 (1.05)^6}{0.12 - 0.05}$$

$$= \$45.95$$

(Alternatively,  $\hat{P}_5 = \$36(1.05)^5_0 = \$45.95$ .) Therefore, Ewald Company's expected stock price 5 years from now,  $\hat{P}_5$ , is \$45.95.

ST-2 a. (1) Calculate the PV of the dividends paid during the supernormal growth period:

$$D_1 = \$1.1500(1.15) = \$1.3225$$

$$D_2 = \$1.3225(1.15) = \$1.5209$$

$$D_3 = \$1.5209(1.13) = \$1.7186$$
PV of Div =  $\$1.3225/(1.12) + \$1.5209/(1.12)^2 + \$1.7186/(1.12)^3$ 

$$= \$3.6167 \approx \$3.62$$

(2) Find the PV of Snyder's stock price at the end of Year 3:

$$\begin{split} \mathring{P}_3 &= \frac{D_4}{r_s - g} = \frac{D_3(1+g)}{r_s - g} \\ &= \frac{\$1.7186(1.06)}{0.12 - 0.06} \\ &= \$30.36 \\ \text{PV of } \mathring{P}_3 &= \$30.36/(1.12)^3 = \$21.61 \end{split}$$

(3) Sum the two components to find the value of the stock today:

$$\hat{P}_0 = \$3.62 + \$21.61 = \$25.23$$

Alternatively, the cash flows can be placed on a time line as follows:

Enter the cash flows into the cash flow register ( $CF_0 = 0$ ,  $CF_1 = 1.3225$ ,  $CF_2 = \frac{1}{\lambda}.5209$ ,  $CF_3 = 32.0803$ ) and I/YR = 12; then press the NPV key to obtain  $\hat{P}_0 = \$25.23$ .

b. 
$$\hat{P}_1 = \$1.5209/(1.12) + \$1.7186/(1.12)^2 + \$30.36/(1.12)^2$$
  
 $= \$26.9311 \approx \$26.93$   
(Calculator solution: \$26.93.)  
 $\hat{P}_2 = \$1.7186/(1.12) + \$30.36/(1.12)$   
 $= \$28.6429 \approx \$28.64$   
(Calculator solution: \$28.64.)

c. Year Dividend Yield + Capital Gains Yield = Total Return
$$1 \quad \frac{\$1.3225}{\$25.23} \approx 5.24\% + \frac{\$26.93 - \$25.23}{\$25.23} \approx 6.74\% \approx 12\%$$

$$2 \quad \frac{\$1.5209}{\$26.93} \approx 5.65\% + \frac{\$28.64 - \$26.93}{\$26.93} \approx 6.35\% \approx 12\%$$

$$3 \quad \frac{\$1.7186}{\$28.64} \approx 6.00\% + \frac{\$30.36 - \$28.64}{\$28.64} \approx 6.00\% \approx 12\%$$

# CHAPTER 8

ST-1 The option will pay off \$60 - \$42 = \$18 if the stock price is up. The option pays off nothing (\$0) if the stock price is down. Find the number of shares in the hedge portfolio:

$$N = \frac{C_u - C_d}{P_u - P_d} = \frac{\$18 - \$0}{\$60 - \$30} = 0.60$$

With 0.6 shares, the stock's payoff will be either 0.6(\$60) = \$36 or 0.6(\$30) = \$18. The portfolio's payoff will be \$36 - \$18 = \$18, or \$18 - \$180 = \$18.

The present value of \$18 at the daily compounded risk-free rate is PV =  $\$18 / [1 + (0.05/365)]^{365} = \$17.12$ . The option price is the current value of the stock in the portfolio minus the PV of the payoff:

$$\begin{split} \text{ST-2} \qquad &V = \ 0.6(\$40) - \$17.12 = \$6.88 \\ d_1 = \frac{\ln(P/X) + [r_{RF} + (\sigma^2/2)]t}{\sigma\sqrt{t}} : \\ &= \frac{\ln(\$22/\$20) + [0.05 + (0.49/2)](0.5)}{0.7\sqrt{0.5}} \\ &= 0.4906 \\ d_2 = d_1 - \sigma(t)^{0.5} = 0.4906 - 0.7(0.5)^{0.5} = -0.0044 \\ N(d_1) = 0.6881 \text{ (from $\textit{Excel NORMSDIST function)}} \\ N(d_2) = 0.4982 \text{ (from $\textit{Excel NORMSDIST function)}} \\ V = P[N(d_1)] - Xe^{-r_{RF}t}[N(d_2)] \\ &= \$22(0.6881) - \$20e^{(-0.05)(0.5)}(0.4982) \\ &= \$5.42 \end{split}$$

# CHAPTER 9

ST-1 a. Component costs are as follows:

Debt at  $r_d = 9\%$ :

$$r_d(1 - T) = 9\%(0.6) = 5.4\%$$

Preferred with F = 5%:

$$r_{ps} = \frac{Preferred\ dividend}{P_{ps}(1-F)} = \frac{\$9}{\$100(0.95)} = 9.5\%.$$

Common with DCF:

$$r_s = \frac{D_1}{P_0} + g = \frac{\$3.922}{\$60} + 6\% = 12.5\%.$$

Common with CAPM:

$$r_s = 6\% + 1.3(5\%) = 12.5\%$$

$$\begin{aligned} \text{b.} \quad \text{WACC} &= w_d r_d (1-T) + w_{ps} r_{ps} + w_s r_s \\ &= 0.25 (9\%) (1-T) + 0.15 (9.5\%) + 0.60 (12.5\%) \\ &= 10.275\% \end{aligned}$$

# CHAPTER 10

#### ST-1 a. Payback:

To determine the payback, construct the cumulative cash flows for each project as follows.

	Cumulative Cash Flows			
Year	Project X	Project Y		
0	-\$10,000	-\$10,000		
1	-3,500	-6,500		
2	-500	-3,000		
3	2,500	500		
4	3,500	4,000		
Payback <sub>X</sub> = $2 + \frac{\$500}{\$3,000} = 2.17 \text{ years}$				
Payback <sub>Y</sub>	$=2+\frac{\$3,000}{\$3,500}=2$	.86 years		

#### Net present value (NPV):

$$\begin{split} NPV_X &= -\$10,\!000 + \frac{\$6,\!500}{(1.12)^1} + \frac{\$3,\!000}{(1.12)^2} + \frac{\$3,\!000}{(1.12)^3} + \frac{\$1,\!000}{(1.12)^4} = \$966.01 \\ NPV_Y &= -\$10,\!000 + \frac{\$3,\!500}{(1.12)^1} + \frac{\$3,\!500}{(1.12)^2} + \frac{\$3,\!500}{(1.12)^3} + \frac{\$3,\!500}{(1.12)^4} = \$630.72 \end{split}$$

Alternatively, using a financial calculator, input the cash flows into the cash flow register, enter I/YR = 12, and then press the NPV key to obtain NPV<sub>X</sub> = 966.01 and NPV<sub>Y</sub> = 630.72.

#### Internal rate of return (IRR):

To solve for each project's IRR, find the discount rates that equate each NPV to zero:

$$IRR_X = 18.0\%$$
  
 $IRR_Y = 15.0\%$ 

#### Modified Internal Rate of Return (MIRR):

To obtain each project's MIRR, begin by finding each project's terminal value (TV) of cash inflows:

$$TV_X = \$6,500(1.12)^3 + \$3,000(1.12)^2 + \$3,000(1.12)^1 + \$1,000 = \$17,255.23$$

$$TV_Y = \$3,500(1.12)^3 + \$3,500(1.12)^2 + \$3,500(1.12)^1 + \$3,500 = \$16,727.65$$

Now, each project's MIRR is the discount rate that equates the PV of the TV to each project's cost, \$10,000:

$$\begin{aligned} \text{MIRR}_{X} &= 14.61\% \\ \text{MIRR}_{Y} &= 13.73\% \end{aligned}$$

#### Profitability index (PI):

To obtain each project's PI, divide its present value of future cash flows by its initial cost. The PV of future cash flows can be found from the NPV calculated earlier:

$$\begin{split} PV_X &= NPV_X + Cost \text{ of } X = \$966.01 + \$10,000 = \$10,966.01 \\ PV_Y &= NPV_Y + Cost \text{ of } Y = \$630.72 + \$10,000 = \$10,630.72 \\ PI_X &= PV_X/Cost \text{ of } X = \$10,966.01/\$10,000 = 1.097 \\ PI_Y &= PV_Y/Cost \text{ of } Y = \$10,630.72/\$10,000 = 1.063 \end{split}$$

b. The following table summarizes the project rankings by each method:

	Project That Ranks Higher
Payback	X
NPV	X
IRR	X
MIRR	X

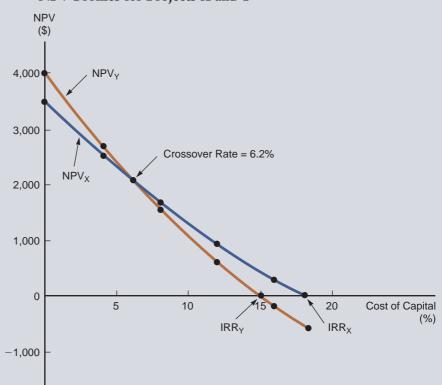
Note that all methods rank Project X over Project Y. Because both projects are acceptable under the NPV, IRR, and MIRR criteria, both should be accepted if they are independent.

- In this case, we would choose the project with the higher NPV at r = 12%, or Project X.
- d. To determine the effects of changing the cost of capital, plot the NPV profiles of each project. The crossover rate occurs at about 6% to 7% (6.2%). See the graph below.

If the firm's cost of capital is less than 6.2%, then a conflict exists because  $NPV_Y > NPV_X$  but  $IRR_X > IRR_Y$ . Therefore, if r were 5% then a conflict would exist. Note, however, that when r = 5.0% we have MIRR<sub>X</sub> = 10.64% and MIRR<sub>y</sub> = 10.83%; hence, the modified IRR ranks the projects correctly even if r is to the left of the crossover point.

e. The basic cause of the conflict is differing reinvestment rate assumptions between NPV and IRR: NPV assumes that cash flows can be reinvested at the cost of capital, whereas IRR assumes that reinvestment yields the (generally) higher IRR. The high reinvestment rate assumption under IRR makes early cash flows especially valuable, so short-term projects look better under IRR.

#### NPV Profiles for Projects X and Y



Cost of Capital	$NPV_X$	$NPV_Y$
0%	\$3,500	\$4,000
4	2,545	2,705
8	1,707	1,592
12	966	631
16	307	(206)
18	5	(585)

#### ST-1 a. Estimated Investment Requirements:

Price	-\$50,000
Modification	-10,000
Change in net working capital	-2,000
Total investment	-\$62,000

#### b. Operating Cash Flows:

	Year 1	Year 2	Year 3
1. After-tax cost savings <sup>a</sup>	\$12,000	\$12,000	\$12,000
2. Depreciation <sup>b</sup>	19,800	27,000	9,000
3. Depreciation tax savings <sup>c</sup>	7,920	10,800	3,600
Operating cash flow $(1 + 3)$	\$19,920	\$22,800	\$15,600

<sup>&</sup>lt;sup>a</sup>\$20,000(1 - T).

#### c. Termination Cash Flow:

Salvage value	\$20,000
Tax on salvage value <sup>a</sup>	-6,320
Net working capital recovery	2,000
Termination cash flow	\$15,680

<sup>&</sup>lt;sup>a</sup>Calculation of tax on salvage value:

Book value = Depreciation basis - Accumulated depreciation = \$60,000 - \$55,800 = \$4,200

Sales price	\$20,000
Less book value	4,200
Taxable income	\$15,800
Tax at 40%	\$ 6,320

<sup>&</sup>lt;sup>b</sup>Depreciable basis = \$60,000; the MACRS percentage allowances are 0.33, 0.45, and 0.15 in Years 1, 2, and 3, respectively; hence, depreciation in Year 1 = 0.33(\$60,000) =\$19,800, and so on. There will remain \$4,200, or 7%, undepreciated after Year 3; it would normally be taken in Year 4.

 $<sup>^{</sup>c}$ Depreciation tax savings = T(Depreciation) = 0.4(\$19,800) = \$7,920 in Year 1, and so forth.

d. **Project NPV:**

$$0 \quad 10\% \quad 1 \quad 2 \quad 3$$
Project Cash Flows  $-62,000 \quad 19,920 \quad 22,800 \quad 31,280$ 

$$NPV = -\$62,000 + \frac{\$19,920}{(1.10)^1} + \frac{\$22,800}{(1.10)^2} + \frac{\$31,280}{(1.10)^3}$$

$$= -\$1,547$$

Alternatively, using a financial calculator, input the cash flows into the cash flow register, enter L/YR = 10, and then press the NPV key to obtain NPV = -\$1,547. Because the earth mover has a negative NPV, it should not be purchased.

#### **ST-2** a. First, find the expected cash flows:

Year		Expected Cash Flows			
0	0.2(-\$100,000)	+ 0.6(-\$100,000)	+ 0.2(-\$100,000)	) =	-\$100,000
1	0.2(\$20,000)	+ 0.6(\$30,000)	+ 0.2(\$40,000)	=	\$ 30,000
2	0.2(\$20,000)	+ 0.6(\$30,000)	+ 0.2(\$40,000)	=	\$ 30,000
3	0.2(\$20,000)	+ 0.6(\$30,000)	+ 0.2(\$40,000)	=	\$ 30,000
4	0.2(\$20,000)	+ 0.6(\$30,000)	+ 0.2(\$40,000)	=	\$ 30,000
5	0.2(\$20,000)	+ 0.6(\$30,000)	+ 0.2(\$40,000)	=	\$ 30,000
5*	0.2(\$0)	+ 0.6(\$20,000)	+ 0.2(\$30,000)	=	\$ 18,000
	0 10% 1	2 3	4	5	
	-\$100,000 30,000	30,000 30,0	00 30,000	48,000	

Next, determine the NPV based on the expected cash flows:

$$NPV = -\$100,000 + \frac{\$30,000}{(1.10)^{1}} + \frac{\$30,000}{(1.10)^{2}} + \frac{\$30,000}{(1.10)^{3}} + \frac{\$30,000}{(1.10)^{3}} + \frac{\$48,000}{(1.10)^{5}} = \$24,900$$

Alternatively, using a financial calculator, input the cash flows in the cash flow register, enter I/YR = 10, and then press the NPV key to obtain NPV = \$24,900.

b. For the worst case, the cash flow values from the cash flow column farthest on the left are used to calculate NPV:

Similarly, for the best case, use the values from the column farthest on the right. Here the NPV is \$70,259.

If the cash flows are perfectly dependent, then the low cash flow in the first year will mean a low cash flow in every year. Thus, the probability of the worst case occurring is the probability of getting the \$20,000 net cash flow in Year 1, or 20%. If the cash flows are independent, then the cash flow in each year can be low, high, or average and so the probability of getting all low cash flows will be

$$(0.2)(0.2)(0.2)(0.2)(0.2) = 0.2^5 = 0.00032 = 0.032\%$$

c. The base-case NPV is found using the most likely cash flows and is equal to \$26,142. This value differs from the expected NPV of \$24,900 because the Year-5 cash flows are not symmetric. Under these conditions, the NPV distribution is as follows:

P	NPV
0.2	-\$24,184
0.6	26,142
0.2	70,259

Thus, the expected NPV is 0.2(-\$24,184) + 0.6(\$26,142) + 0.2(\$70,259) =\$24,900. As is always the case, the expected NPV is the same as the NPV of the expected cash flows found in part a. The standard deviation is \$29,904:

$$\begin{split} \sigma_{NPV}^2 &= 0.2 (-\$24,184 - \$24,900)^2 + 0.6 (\$26,142 - \$24,900)^2 \\ &+ 0.2 (\$70,259 - \$24,900)^2 \\ &= \$894,261,126 \\ \sigma_{NPV} &= \sqrt{\$894,261,126} = \$29,904. \end{split}$$

The coefficient of variation, CV, is \$29,904/\$24,900 = 1.20.

# CHAPTER 12

ST-1 To solve this problem, we first define  $\Delta S$  as the change in sales and g as the growth rate in sales. Then we use the three following equations:

$$\begin{array}{l} \Delta S = S_0 g \\ S_1 = S_0 (1+g) \\ AFN = (A^*/S_0)(\Delta S) - (L^*/S_0)(\Delta S) - MS_1 (1-Payout\ ratio) \end{array}$$

Set AFN = 0; substitute in known values for  $A^*/S_0$ ,  $L^*/S_0$ , M, d, and  $S_0$ ; and then solve for g:

$$0 = 1.6(\$100g) - 0.4(\$100g) - 0.10[\$100(1+g)](0.55)$$

$$= \$160g - \$40g - 0.055(\$100 + \$100g)$$

$$= \$160g - \$40g - \$5.5 - \$5.5g$$

$$\$114.5g = \$5.5$$

$$g = \$5.5/\$114.5 = 0.048 = 4.8\%$$

$$= \text{Maximum growth rate without external financing}$$

ST-2 Assets consist of cash, marketable securities, receivables, inventories, and fixed assets. Therefore, we can break the A\*/S<sub>0</sub> ratio into its components cash/sales, inventories/sales, and so forth. Then,

$$\frac{A^*}{S_0} = \frac{A^* - Inventories}{S_0} + \frac{Inventories}{S_0} = 1.6$$

We know that the inventory turnover ratio is sales/inventories = 3 times, so inventories/sales = 1/3 = 0.3333. Further, if the inventory turnover ratio can be increased to 4 times, then the inventory/sales ratio will fall to 1/4 = 0.25, a difference of 0.3333 - 0.2500 = 0.0833. This, in turn, causes the A\*/S<sub>0</sub> ratio to fall from  $A^*/S_0 = 1.6$  to  $A^*/S_0 = 1.6 - 0.0833 = 1.5167$ . This change has two effects: First, it changes the AFN equation; and second, it means that Barnsdale currently has excessive inventories. Because it is costly to hold excess inventories, Barnsdale will want to reduce its inventory holdings by not replacing inventories until the excess amounts have been used. We can account for this by setting up the revised AFN equation (using the new A\*/S<sub>0</sub> ratio), estimating the funds that will be needed next year if no excess inventories are currently on hand, and then subtracting out the excess inventories that are currently on hand:

#### **Present Conditions:**

$$\frac{\text{Sales}}{\text{Inventories}} = \frac{\$100}{\text{Inventories}} = 3$$

SO

Inventories = \$100/3 = \$33.3 million at present

#### **New Conditions:**

$$\frac{\text{Sales}}{\text{Inventories}} = \frac{\$100}{\text{Inventories}} = 4$$

so

New level of inventories = \$100/4 = \$25 million

Therefore,

Excess inventories = 
$$$33.3-$25 = $8.3$$
 million

#### Forecast of Funds Needed, First Year:

$$\Delta S$$
 in first year = 0.2(\$100 million) = \$20 million  
AFN = 1.5167(\$20) - 0.4(\$20) - 0.1(0.55)(\$120)-\$8.3  
= \$30.3 - \$8 - \$6.6 - \$8.3  
= \$7.4 million

#### Forecast of Funds Needed, Second Year:

$$\Delta S$$
 in second year =  $gS_1 = 0.2(\$120 \text{ million}) = \$24 \text{ million}$   
AFN =  $1.5167(\$24) - 0.4(\$24) - 0.1(0.55)(\$144)$   
=  $\$36.4 - \$9.6 - \$7.9$   
=  $\$18.9 \text{ million}$ 

ST-3 a. Full capacity sales = 
$$\frac{\text{Current sales}}{\text{Percentage of capacity at which}} = \frac{\$36,000}{0.75} = \$48,000$$
FA were operated

Percentage increase = 
$$\frac{\text{New sales - Old sales}}{\text{Old sales}} = \frac{\$48,000 - \$36,000}{\$36,000} = 0.33$$

Therefore, sales could expand by 33% before Van Auken Lumber would need to add fixed assets.

b.

### Van Auken Lumber: Projected Income Statement for December 31, 2011 (Thousands of Dollars)

	2010	FORECAST BASIS	2011
Sales	\$36,000	1.25(Sales <sub>10</sub> )	\$45,000
Operating costs	30,783	85.508%(Sales <sub>11</sub> )	38,479
EBIT	\$ 5,217		\$ 6,521
Interest	<u>717</u>	12%(Debt <sub>10</sub> )	1,017
EBT	\$ 4,500		\$ 5,504
Taxes (40%)	1,800		2,202
Net income	\$ 2,700		\$ 3,302
Dividends (60%)	\$ 1,620		\$ 1,981
Additions to RE	\$ 1,080		\$ 1,321

### Van Auken Lumber: Projected Balance Sheet for December 31, 2011 (Thousands of Dollars)

(modsands of bondis)		PERCENT OF 2011	Γ			2011 AFTER
	2010		ADDITIONS	2011	AFN	AFN
Cash	\$ 1,800	5.000%		\$ 2,250		\$ 2,250
Receivables	10,800	30.000		13,500		13,500
Inventories	12,600	35.000		15,750		15,750
Total current assets	\$25,200			\$31,500		\$31,500
Net fixed assets	21,600			21,600 <sup>a</sup>		21,600
Total assets	\$46,800			\$53,100		\$53,100
Accounts payable	\$ 7,200	20.000		\$ 9,000		\$ 9,000
Notes payable	3,472			3,472	+2,549	6,021
Accruals	2,520	7.000		3,150		3,150
Total current liabilities	\$13,192			\$15,622		\$18,171
Mortgage bonds	5,000			5,000		5,000
Common stock	2,000			2,000		2,000
Retained earnings	26,608		1,321 <sup>b</sup>	27,929		27,929
Total liabilities and equity	\$46,800			\$50,551		\$53,100
AFN =				\$ 2,549		

<sup>&</sup>lt;sup>a</sup>From part a we know that sales can increase by 33% before additions to fixed assets are needed. <sup>b</sup>See income statement

# CHAPTER 13

ST-1 a. 
$$V_{op} = \frac{FCF(1+g)}{WACC-g} = \frac{\$100,000(1+0.07)}{0.11-0.07} = \$2,675,000$$

- b. Total value = Value of operations + Value of nonoperating assets = \$2,675,000 + \$325,000 = \$3,000,000
- c. Value of equity = Total value – Value of debt = \$3,000,000 - \$1,000,000 = \$2,000,000
- d. Price per share = Value of equity ÷ Number of shares = \$2,000,000/50,000 = \$40

$$DPS = \$2,600,000/1,000,000 \text{ shares} = \$2.60$$

# CHAPTER 15

ST-1 a. 
$$S = P(n) = \$30(600,000) = \$18,000,000$$
  
 $V = D + S = \$2,000,000 + \$18,000,000 = \$20,000,000$ 

$$\begin{array}{ll} b. & w_d = D/V = \$2,000,000/\$20,000,000 = 0.10 \\ & w_s = S/V = \$18,000,000/\$20,000,000 = 0.90 \\ & WACC = w_d \ r_d(1-T) + w_s \ r_s \\ & = (0.10)(10\%)(0.60) + (0.90)(15\%) = 14.1\% \end{array}$$

c. WACC = 
$$(0.50)(12\%)(0.60) + (0.50)(18.5\%) = 12.85\%$$
  
Since g = 0, it follows that FCF = NOPAT.

$$\begin{aligned} V_{opNew} &= FCF/WACC = EBIT(1-T)/0.1285 = \$4,\!700,\!000(0.60)/0.1285 \\ &= \$21,\!945,\!525.292 \end{aligned}$$

$$D = w_d(V_{op}) = 0.50(\$21,945,525.292) = \$10,972,762.646$$

Since it started with \$2 million debt, it will issue

$$D_{New} - D_{Old} = \$8,972,762.646 = \$10,972,762.646 - \$2,000,000.$$

$$S_{Post} = V_{opNew} - D_{New} = \$21,945,525.292 - \$10,972,762.646 = \$10,972,762.646$$

(Alternatively, 
$$S_{Post} = w_s(V_{opNew}) = 0.50(\$21,945,525.292) = \$10,972,762.646$$

$$\begin{split} n_{Post} &= n_{Prior} \bigg[ \frac{V_{opNew} - D_{New}}{V_{opNew} - D_{Old}} \bigg] \\ &= 600,\!000 \bigg[ \frac{\$21,\!945,\!525.292 - \$10,\!972,\!762.646}{\$21,\!945,\!525.292 - \$2,\!000,\!000} \bigg] \\ &= 600,\!000 \bigg[ \frac{\$10,\!972,\!762.646}{\$19,\!945,\!525.292} \bigg] \\ &= 330,\!082 \end{split}$$

$$\begin{split} P_{Post} &= (V_{opNew} - D_{Old})/n_{Prior} \\ &= (\$21,945,525.292 - \$2,000,000)/600,000 \\ &= \$33.2425 \end{split}$$

Alternatively, after issuing debt and before repurchasing stock, the firm's equity,  $S_{Prior}$ , is worth  $V_{opNew} + (D_{New} - D_{Old}) - D_{New} = $21,945,525.292$ +\$8,972,762.646 -\$10,972,762.646 =\$19,945,525.29. The stock price prior to the repurchase is  $P_{Prior} = S_{Prior} / n_{Prior} = $19,945,525.29/600,000 =$ \$33.242542. The firm used the proceeds of the new debt, \$8,972,762.646, to repurchase X shares of stock at a price of \$33.242542 per share. The number of shares it will repurchase is X = \$8,972,762.646/\$33.242542 =269,918.07. Thus, there are 600,000 - 269,918.07 = 330,082 shares remaining. As a check, the stock price should equal the market value of equity (S) divided by the number of shares:  $P_0 = \$10,972,762.646/330,082$ = \$33.2425.

ST-2 a. LIC's current cost of equity is

$$r_s = 6\% + 1.5(4\%) = 12\%$$

b. LIC's unlevered beta is

$$b_{\rm U} = 1.5/[1 + (1 - 0.40)(25\%/75\%)] = 1.5/1.2 = 1.25$$

c. LIC's levered beta at D/S = 60%/40% = 1.5 is

$$b = 1.25[1 + (1 - 0.40)(60/40)] = 2.375$$

LIC's new cost of capital will be

$$r_s = 6\% + (2.375)(4\%) = 15.5\%$$

# CHAPTER 16

#### ST-1 The Calgary Company: Alternative Balance Sheets

	RESTRICTED (40%)	MODERATE (50%)	RELAXED (60%)
Current assets (% of sales)	\$1,200,000	\$1,500,000	\$1,800,000
Fixed assets	600,000	600,000	600,000
Total assets	\$1,800,000	\$2,100,000	\$2,400,000
Debt	\$ 900,000	\$1,050,000	\$1,200,000
Equity	900,000	1,050,000	1,200,000
Total liabilities and equity	\$1,800,000	\$2,100,000	\$2,400,000

	, , , , , , , , , , , , , , , , , , , ,		
	RESTRICTED	MODERATE	RELAXED
Sales	\$3,000,000	\$3,000,000	\$3,000,000
EBIT	450,000	450,000	450,000
Interest (10%)	90,000	105,000	120,000
Earnings before taxes	\$ 360,000	\$ 345,000	\$ 330,000
Taxes (40%)	144,000	138,000	132,000
Net income	\$ 216,000	\$ 207,000	\$ 198,000
ROE	24.0%	19.7%	16.5%

The Calgary Company: Alternative Income Statements

ST-2 a. and b.

#### Income Statements for Year Ended December 31, 2010 (Thousands of Dollars)

	VANDERHEIDEN PRESS			NHOUSE SHING
	a	b	a	b
EBIT	\$ 30,000	\$ 30,000	\$ 30,000	\$ 30,000
Interest	12,400	14,400	10,600	18,600
Taxable income	\$ 17,600	\$ 15,600	\$ 19,400	\$ 11,400
Taxes (40%)	7,040	6,240	7,760	4,560
Net income	\$ 10,560	\$ 9,360	\$ 11,640	\$ 6,840
Equity	\$100,000	\$100,000	\$100,000	\$100,000
Return on equity	10.56%	9.36%	11.64%	6.84%

The Vanderheiden Press has a higher ROE when short-term interest rates are high, whereas Herrenhouse Publishing does better when rates are lower.

c. Herrenhouse's position is riskier. First, its profits and return on equity are much more volatile than Vanderheiden's. Second, Herrenhouse must renew its large short-term loan every year, and if the renewal comes up at a time when money is tight or when its business is depressed or both, then Herrenhouse could be denied credit, which could put it out of business.

# CHAPTER 17

ST-1 
$$\frac{\text{Euros}}{\text{C$\$}} = \frac{\text{Euros}}{\text{US$\$}} \times \frac{\text{US$\$}}{\text{C$\$}}$$
$$= \frac{0.98}{\$1} \times \frac{\$1}{1.5} = \frac{0.98}{1.5} = 0.6533 \text{ euros per Canadian dollar}$$

#### (ST-1) a. Cost of Leasing:

	YEAR 0	YEAR 1	YEAR 2	YEAR 3	YEAR 4
Lease payment	-\$10,000	-\$10,000	-\$10,000	-\$10,000	\$0
Payment tax savings	4,000	4,000	4,000	4,000	0
Net cash flow	-\$ 6,000	-\$ 6,000	-\$ 6,000	-\$ 6,000	\$0
PV cost of leasing @ 6% =	-\$22,038				

#### b. Cost of Owning:

In our solution, we will consider the \$40,000 cost as a Year-0 outflow rather than including all the financing cash flows. The net effect is the same because the PV of the financing flows, when discounted at the after-tax cost of debt, is the cost of the asset.

	YEAR 0	YEAR 1	YEAR 2	YEAR 3	YEAR 4
Net purchase price	-\$40,000				
Maintenance cost		-\$1,000	-\$1,000	-\$1,000	-\$1,000
Maintenance tax savings		400	400	400	400
Depreciation tax savings		5,280	7,200	2,400	1,120
Residual value					10,000
Residual value tax					<del>-4,000</del>
Net cash flow	- <u>\$40,000</u>	\$4,680	\$6,600	\$1,800	\$6,520

PV cost of owning @ 6% = -\$23,035

Since the present value of the cost of leasing is less than the present value of the cost of owning, the truck should be leased. Specifically, the NAL is \$23,035 - \$22,038 = \$997.

c. Use the cost of debt because most cash flows are fixed by contract and thus are relatively certain; therefore, lease cash flows have about the same risk as the firm's debt. Also, leasing is considered as a substitute for debt. Use an after-tax cost rate to account for interest tax deductibility.

# CHAPTER 19

ST-1 First issue: 10-year straight bonds with a 6% coupon.

> Second issue: 10-year bonds with 4.5% annual coupon with warrants. Both bonds issued at par 1,000. Value of warrants = 3

> First issue: N = 10, PV = -1000, PMT = 60, and FV = 1000; then solve for  $I/YR = r_d = 6\%$ . (Since it sold for par, we should know that  $r_d = 6\%$ .)

> Second issue: \$1,000 = Bond + Warrants. This bond should be evaluated at 6% (since we know the first issue sold at par) in order to determine its present value: N = 10,  $I/YR = r_d = 6$ , PMT = 45, and FV = 1000; then solve for PV = \$889.60.

> The value of the warrants can be determined as the difference between \$1,000 and the second bond's present value:

> > Value of warrants = \$1.000 - \$889.6 = \$110.40.

- ST-1 a. Proceeds per share = (1 - 0.07)(\$20) = \$18.60. Required proceeds after direct costs: \$30 million + \$800,000 = \$30.8 million.Number of shares = \$30.8 million/\$18.60 per share = 1.656 millionshares.
  - b. Amount left on table = (Closing price offer price)(Number of shares) = (\$22 - \$20)(1.656 million) = \$3.312 million.
  - c. Underwriting cost = 0.07(\$20)(1.656) = \$2.318 million. Total costs = \$0.800 + \$2.318 + \$3.312 = \$6.430 million.

# CHAPTER 21

ST-1 a. The unlevered cost of equity based on the pre-merger required rate of return and pre-merger capital structure is

$$\begin{aligned} r_{sU} &= w_d r_d + w_s r_{sL} \\ &= 0.25(6\%) + 0.75(10\%) \\ &= 9\% \end{aligned}$$

The post-horizon levered cost of equity is

$$\begin{split} r_{sL} &= r_{sU} + (r_{sU} - r_d)(D/S) \\ &= 9\% + (9\% - 7\%)(0.35/0.65) \\ &= 10.077\% \\ WACC &= w_d r_d (1 - T) + w_s r_s \\ &= 0.35(7\%)(1 - 0.40) + 0.65(10.077\%) \\ &= 8.02\% \end{split}$$

b. The horizon value of unlevered operations is

Horizon value 
$$HV_{U,3} = FCF_3(1+g)/(r_{sU}-g)$$
  
=  $[\$25(1.05)]/(0.09-0.05)$   
=  $\$656.250$  million

Unlevered 
$$V_{ops} = \frac{\$10}{(1.09)^1} + \frac{\$20}{(1.09)^2} + \frac{\$25 + \$656.25}{(1.09)^3}$$
  
= \\$552.058 million

Tax shields in Years 1 through 3 are

Tax shield = Interest 
$$\times$$
 T  
TS<sub>1</sub> = \$28.00(0.40) = \$11.200 million  
TS<sub>2</sub> = \$24.00(0.40) = \$9.600 million  
TS<sub>3</sub> = \$20.28(0.40) = \$8.112 million

Horizon value 
$$HV_{TS,3} = TS_3(1+g)/(r_{sU}-g)$$
  
=  $[\$8.112(1.05)]/(0.09-0.05)$   
=  $\$212.940$  million

Value of tax shield = 
$$\frac{\$11.2}{(1.09)^1} + \frac{\$9.6}{(1.09)^2} + \frac{\$8.112 + \$212.940}{(1.09)^3}$$
  
=  $\$189.048$  million

Total value = Unlevered  $V_{ops} + Value$  of tax shield = \$552.058 + \$189.048= \$741.106.

# CHAPTER 22

ST-1 a. Distribution to priority claimants (millions of dollars):

<ol> <li>First mortgage (paid from sale of fixed assets)</li> <li>Second mortgage (paid from sale of fixed assets after satisfying first mortgage: \$750 - \$700 = \$50)</li> </ol>	0
	0
, ,	0
3. Fees and expenses of bankruptcy	1
4. Wages due to workers	0
5. Taxes due	0
Funds available for distribution to general creditors <u>\$ 24</u>	.9

b. Distribution to general creditors (millions of dollars):

GENERAL CREDITOR CLAIMS	AMOUNT OF CLAIM	PRO RATA DISTRIBUTION <sup>a</sup>	DISTRIBUTION AFTER SUBORDINATE ADJUSTMENT <sup>b</sup>	% OF ORIGINAL CLAIM RECEIVED
Unsatisfied second mortgage	\$ 350	\$ 60	\$ 60	28%°
Accounts payable	100	17	17	17
Notes payable	300	52	86	29
Debentures	500	86	86	17
Subordinated debentures	200	34	0	0
Total	<u>\$1,450</u>	<u>\$249</u>	<u>\$249</u>	

Total distribution to second mortgage holders: \$50 + \$60 = \$110 million.

Total distribution to holders of notes payable: \$86 million.

Total distribution to holders of subordinated debentures: \$0 million.

Total distribution to common stockholders: \$0 million.

<sup>&</sup>lt;sup>a</sup>Pro rata distribution: \$249/\$1,450 = 0.172 = 17.2%.

<sup>&</sup>lt;sup>b</sup>Subordinated debentures are subordinated to notes payable. Unsatisfied portion of notes payable is greater than subordinated debenture distribution, so subordinated debentures receive \$0.

<sup>&</sup>lt;sup>c</sup>Includes \$50 from sale of fixed assets received in priority distribution.

- ST-1 a. The hypothetical bond in the futures contract has an annual coupon of 6% (paid semiannually) and a maturity of 20 years. At a price of 97'13 (this is the percent of par), a \$1,000 par bond would have a price of 1,000(97 + 13/32)/100 = 974.0625. To find the yield: N = 40, PMT = 30, FV = 1000, PV = -974.0625; then I = 3.1143% per 6 months. The nominal annual yield is 2(3.1143%) = 6.2286%.
  - b. In this situation, the firm would be hurt if interest rates were to rise by September, so it would use a short hedge or sell futures contracts. Because futures contracts are for \$100,000 in Treasury bonds, the value of a futures contract is \$97,406.25 and the firm must sell 5,000,000/ $97,406.25 = 51.33 \approx 51$  contracts to cover the planned \$5,000,000 September bond issue. Because futures maturing in June are selling for 97 13/32 of par, the value of Wansley's futures is about 51(\$97,406.25) = \$4,967,718.75. Should interest rates rise by September, Wansley will be able to repurchase the futures contracts at a lower cost, which will help offset their loss from financing at the higher interest rate. Thus, the firm has hedged against rising interest rates.
  - c. The firm would now pay 13% on the bonds. With a 12% coupon rate, the PV of the new issue is only \$4,646,361.83 (N = 40, I = 13/2 = 6.5, PMT = -0.12/2(5000000) = -300000, FV = -5000000; then solve for PV). Therefore, the new bond issue would bring in only \$4,646,361.83, so the cost of the bond issue that is due to rising rates is \$5,000,000 -\$4,646,361.83 = \$353,638.17.

However, the value of the short futures position began at \$4,967,718.75. Now, if interest rates increased by 1 percentage point, then the yield on the futures would go up to 7.2286% (7.2286 = 6.2286 + 1). To find the value of the futures contract, enter N = 40, I = 7.2286/2 = 3.6143 (from part a), PMT = 3000, and FV = 100000; then solve for PV = \$87,111.04 per contract. With 51 contracts, the value of the futures position is \$4,442,663.04. (*Note:* If you don't round off in any previous calculations, then the PV comes to \$4,442,668.38.)

Because Wansley Company sold the futures contracts for \$4,967,718.75 and will, in effect, buy them back at \$4,442,668.04, the firm would make a profit of \$4,967,718.75 - \$4,442,668.04 = \$525,050.71 profit on the transaction (if we ignore transaction costs).

Thus, the firm gained \$525,050.71 on its futures position, but lost \$353,638.17 on its underlying bond issue. On net, it gained \$525,050.71 -\$353,638.17 = \$171,412.54.

# CHAPTER 24

ST-1 a. For Security A:

$\mathbf{P}_{\mathbf{A}}$	$\mathbf{r}_{\mathbf{A}}$	$P_A r_A$	$(\mathbf{r}_{\mathbf{A}} - \overset{\wedge}{\mathbf{r}}_{\mathbf{A}})$	$(\mathbf{r}_{\mathbf{A}} - \mathring{\mathbf{r}}_{\mathbf{A}})^2$	$P_A(r_A - \mathring{r}_A)^2$
0.1	-10%	-1.0%	-25%	625	62.5
0.2	5	1.0	-10	100	20.0
0.4	15	6.0	0	0	0.0
0.2	25	5.0	10	100	20.0
0.1	40	4.0	25	625	<u>62.5</u>
	$\overset{\wedge}{r}_{A}$	= 15.0%			$\sigma_{A} = \sqrt{165.0} = 12.8\%$

$$\begin{aligned} w_A &= \frac{\sigma_B(\sigma_B - \rho_{AB}\sigma_A)}{\sigma_A^2 + \sigma_B^2 - 2\rho_{AB}\sigma_A\sigma_B} \\ &= \frac{25.7[25.7 - (-0.5)(12.8)]}{(12.8)^2 + (25.7)^2 - 2(-0.5)(12.8)(25.7)} \\ &= \frac{824.97}{1.153.29} = 0.7153. \end{aligned}$$

or 71.53% invested in A and 28.47% invested in B.

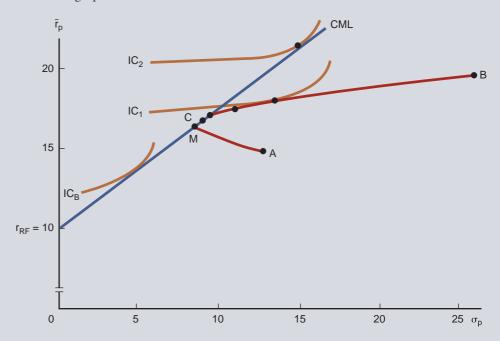
$$\begin{split} &\sigma_p = \sqrt{(w_A \sigma_A)^2 + (1 - w_A)^2 (\sigma_B)^2 + 2 w_A (1 - w_A) \rho_{AB} \sigma_A \sigma_B} \\ &= \sqrt{(0.75)^2 (12.8)^2 + (0.25)^2 (25.7)^2 + 2(0.75) (0.25) (-0.5) (12.8) (25.7)} \\ &= \sqrt{92.16 + 41.28 - 61.68} \\ &= \sqrt{71.76} = 8.47\% \text{ when } w_A = 75\% \\ &\sigma_p = \sqrt{(0.7153)^2 (12.8)^2 + (0.2847)^2 (25.7)^2 + 2(0.7153) (0.2847) (-0.5) (12.8) (25.7)} \\ &= 8.38\% \text{ when } w_A = 71.53\% \text{ (this is the minimum } \sigma_P) \\ &\sigma_p = \sqrt{(0.5)^2 (12.8)^2 + (0.5)^2 (25.7)^2 + 2(0.5) (0.5) (-0.5) (12.8) (25.7)} \\ &= 11.3\% \text{ when } w_A = 50\% \\ &\sigma_p = \sqrt{(0.25)^2 (12.8)^2 + (0.75)^2 (25.7)^2 + 2(0.25) (0.75) (-0.5) (12.8) (25.7)} \\ &= 17.89\% \text{ when } w_A = 25\% \end{split}$$

% in A	% in B	${\bf \hat{r}_p}$	$\sigma_{\mathbf{p}}$
100%	0%	15.00%	12.8%
75	25	16.25	8.5
71.53	28.47	16.42	8.4
50	50	17.50	11.1
25	75	18.75	17.9
0	100	20.00	25.7

#### Calculations for preceding table:

$$\begin{split} & \mathring{r}_p = w_A(\mathring{r}_A) + (1-w_A) \ (\mathring{r}_B) \\ & = 0.75(15) + (0.25)(20) \\ & = 0.7153(15) + 0.2847(20) = 16.25\% \quad \text{when } w_A = 75\% \\ & = 0.7153(15) + 0.2847(20) = 16.42\% \quad \text{when } w_{A0} = 71.53\% \\ & = 0.5(15) + 0.5(20) \\ & = 17.50\% \quad \text{when } w_A = 50\% \\ & = 0.25(15) + 0.75(20) \\ & = 18.75\% \quad \text{when } w_A = 25\% \end{split}$$

d. See graph below.



See indifference curve IC<sub>1</sub> in the preceding graph. At the point where  $\hat{r}_{p} = 18\%, \, \sigma_{p} = 13.5\%.$ 

$$\begin{split} \hat{r}_p &= w_A (\hat{r}_A) + (1 - w_A) (\hat{r}_B) \\ 18 &= w_A (15) + (1 - w_A) (20) \\ &= 15 w_A + 20 - 20 w_A \\ 5 w_A &= 2 \\ w_A &= 0.4 \text{ or } 40\%. \end{split}$$

Therefore, to an approximation, your optimal portfolio would have 40% in A and 60% in B, with  $\hat{r}_p = 18\%$  and  $\sigma_p = 13.5\%$ . (We could get an exact  $\sigma_p$  by using  $w_A = 0.4$  in the equation for  $\sigma_p$ .)

f. The existence of the riskless asset would enable you to go to the CAPM. We would draw in the CML as shown on the graph in part d. Now you would hold a portfolio of stocks, borrowing on margin to hold more stocks than your net worth, and move to a higher indifference curve, IC<sub>2</sub>.

You can put all of your money into the riskless asset, all in A, all in B, or some in each security. The most logical choices are (1) hold a portfolio of A and B plus some of the riskless asset, (2) hold only a portfolio of A and B, or (3) hold a portfolio of A and B and borrow to leverage the portfolio, assuming you can borrow at the riskless rate.

Reading from the graph, we see that your  $\hat{r}_p$  at the point of tangency between your IC<sub>2</sub> and the CML is about 22%. We can use this information to find out how much you invest in the market portfolio and how much you invest in the riskless asset. (It will turn out that you have a *negative* investment in the riskless asset, which means that you borrow rather than lend at the risk-free rate.)

$$\begin{array}{l} {\displaystyle \stackrel{\wedge}{r_{p}}=w_{RF}(r_{RF})+(1-w_{RF})(\stackrel{\wedge}{r_{M}})}\\ 22=w_{RF}(10)+(1-w_{RF})(16.8)\\ =10w_{RF}+16.8-16.8w_{RF}\\ -6.8w_{RF}=5.2\\ w_{RF}=-0.76 \text{ or } -76\% \text{ (which means that you borrow)}\\ 1-w_{RF}=1.0-(-0.76)\\ =+1.76 \text{ or } 176\% \text{ in the market portfolio} \end{array}$$

Hence this investor, with \$200,000 of net worth, buys stock with a value of \$200,000(1.76) = \$352,000 and borrows \$152,000.

The risk of this leveraged portfolio is

$$\begin{split} \sigma_p &= \sqrt{(-0.76)^2(0)^2 + (1.76)^2(8.5)^2 + 2(-0.76)(1.76)(0)(8.5)(0)} \\ &= \sqrt{(1.76)^2(8.5)^2} \\ &= (1.76)(8.5) = 15\% \end{split}$$

Your indifference curve suggests that you are not very risk averse. A risk-averse investor would have a steep indifference curve (visualize a set of steep curves that were tangent to CML to the left of Point C). This investor would hold some of A and B, combined to form portfolio M, and some of the riskless asset.

g. Given your assumed indifference curve, you would, when the riskless asset becomes available, change your portfolio from the one found in part e (with  $\mathring{r}_p = 18\%$  and  $\sigma_p = 13.5\%$ ) to one with  $\mathring{r}_p \approx 22.0\%$  and  $\sigma_p \approx 15.00\%$ .

$$\begin{array}{ll} h. & r_A = r_{RF} + (r_M - r_{RF})b_A \\ 15 = 10 + (16.8 - 10)b_A \\ & = 10 + (6.8)b_A. \\ b_A = 0.74. \\ 20 = 10 + (6.8)b_B \\ b_B = 1.47 \end{array}$$

Note that the 16.8% value for  $r_{\rm M}$  was approximated from the graph. Also, this solution assumes that you can borrow at r<sub>RF</sub> = 10%. This is a basic but questionable—CAPM assumption. If the borrowing rate is above r<sub>RF</sub>, then the CML would turn down to the right of Point M.

# CHAPTER 25

#### ST-1 a. NPV of each demand scenario:

		Future C	ash Flows	NPV This	Probability
0	Probability	Year 1	Year 2	Scenario	$\times$ NPV
		\$13	\$13	\$13.13	\$3.28
	25%				
-\$8	50%	\$7	\$7	\$3.38	\$1.69
	25%				
	*	\$1	\$1	-\$6.37	-\$1.59
		Ex	\$3.38		

NPV under high-demand scenario:

$$NPV = -\$8 + \frac{\$13}{(1+0.15)^1} + \frac{\$13}{(1+0.15)^2} = \$13.13$$

NPV under medium-demand scenario:

$$NPV = -\$8 + \frac{\$7}{(1+0.15)^1} + \frac{\$7}{(1+0.15)^2} = \$3.38$$

NPV under low-demand scenario:

NPV = 
$$-\$8 + \frac{\$1}{(1+0.15)^1} + \frac{\$1}{(1+0.15)^2} = -\$6.37$$

Expected NPV = 0.25(\$13.13) + 0.50(\$3.38) + 0.25(-\$6.37) = \$3.38 million.

b. NPV of operating cash flows if the additional project is implemented only when optimal:

	Future Ope	rating Cash F	lows (Discour	nt at WACC)	NPV This	Probability
Probability	Year 1	Year 2	Year 3	Year 4	Scenario	× NPV
1	\$13	\$13	\$13	\$13	\$37.11	\$9.28
25%						
50% ──►	\$7	\$7	\$7	\$7	\$19.98	\$9.99
25% _						
*	\$1	\$1	\$0	\$0	\$1.63	\$0.41

Expected NPV of future operating CFs = \$19.68

NPV of operating cash flows under high-demand scenario:

$$NPV = \frac{\$13}{(1+0.15)^1} + \frac{\$13}{(1+0.15)^2} + \frac{\$13}{(1+0.15)^3} + \frac{\$13}{(1+0.15)^4} = \$37.11$$

NPV of operating cash flows under medium-demand scenario:

$$NPV = \frac{\$7}{\left(1 + 0.15\right)^{1}} + \frac{\$7}{\left(1 + 0.15\right)^{2}} + \frac{\$7}{\left(1 + 0.15\right)^{3}} + \frac{\$7}{\left(1 + 0.15\right)^{4}} = \$19.98$$

NPV of operating cash flows under low-demand scenario:

NPV = 
$$\frac{\$1}{(1+0.15)^1} + \frac{\$1}{(1+0.15)^2} = \$1.63$$

Expected NPV of operating cash flows = 0.25(\$37.11) + 0.50(\$19.98)+0.25(\$1.63)= \$19.68 million

Find NPV of costs, discounted at risk-free rate:

#### Cost of Implementing Project Now and Additional Project at Year 2 (Discount at Risk-Free Rate)

0	Probability	Year 1	Year 2	NPV This Scenario	Probability × NPV
		\$0	-\$8	-\$15.12	-\$3.78
	25%				
-\$8	50%	\$0	-\$8	-\$15.12	-\$7.56
	25% <				
	*	\$0	\$0	-\$8.00	-\$2.00
		Expected NPV of future operating CEs –			-\$13.34

Expected NPV of future operating CFs =

NPV of costs under high-demand scenario:

NPV = 
$$-\$8 + \frac{\$0}{(1+0.06)^1} + \frac{-\$8}{(1+0.06)^2} = -\$15.12$$

NPV of costs under medium-demand scenario:

$$NPV = -\$8 + \frac{\$0}{(1+0.06)^1} + \frac{-\$8}{(1+0.06)^2} = -\$15.12$$

NPV of costs under low-demand scenario:

$$NPV = -\$8 + \frac{\$0}{(1+0.06)^1} + \frac{\$0}{(1+0.06)^2} = -\$8.00$$

Expected NPV of costs = 
$$0.25(-\$15.12) + 0.50(-\$15.12) + 0.25(-\$8.00)$$
  
=  $-\$13.34$  million

Expected NPV of project = Expected NPV of operating cash flows - Expected NPV of costs 
$$= \$19.68 - \$13.34 = \$6.34$$

c. Find the expected NPV of the additional project's operating cash flows, which is analogous to the "stock price" in the Black-Scholes model:

#### **Future Operating Cash Flows of Additional** Project (Discount at WACC)

0	Probability	Year 1	Ye ar 2	Year 3	Ye ar 4	NPV of This Scenario	Probability × NPV
		\$0	\$0	\$13	\$13	\$15.98	\$4.00
	25%						
	50% →	\$0	\$0	\$7	\$7	\$8.60	\$4.30
	25% <						
	*	\$0	\$0	\$1	\$1	\$1.23	\$0.31

Expected NPV future operating CFs =

\$8.60

NPV of operating cash flows under high-demand scenario:

$$NPV = \frac{\$0}{(1+0.15)^1} + \frac{\$0}{(1+0.15)^2} + \frac{\$13}{(1+0.15)^3} + \frac{\$13}{(1+0.15)^4} = \$15.98$$

NPV of operating cash flows under medium-demand scenario:

$$NPV = \frac{\$0}{\left(1 + 0.15\right)^{1}} + \frac{\$0}{\left(1 + 0.15\right)^{2}} + \frac{\$7}{\left(1 + 0.15\right)^{3}} + \frac{\$7}{\left(1 + 0.15\right)^{4}} = \$8.60$$

NPV of operating cash flows under low-demand scenario:

NPV = 
$$\frac{\$0}{(1+0.15)^1} + \frac{\$0}{(1+0.15)^2} + \frac{\$1}{(1+0.15)^3} + \frac{\$1}{(1+0.15)^4} = \$1.23$$

The inputs for the Black-Scholes model are:  $r_{RF} = 0.06$ , X = 8, P = 8.6, t = 2, and  $\sigma^2 = 0.150$ . Using these inputs, the value of the option, V, is

$$\begin{split} d_1 &= \frac{ln(P/X) + \left[r_{RF} + \frac{\sigma^2}{2}\right] \times t}{\sigma\sqrt{t}} = \frac{ln(8.6/8) + \left[0.06 + \frac{0.150}{2}\right] \times 2}{\sqrt{0.15}\sqrt{2}} = 0.62499 \\ d_2 &= d_1 - \sigma\sqrt{t} = 0.62499 - \sqrt{0.15}\sqrt{2} = 0.07727 \end{split}$$

Use Excel's NORMSDIST function to calculate N(d<sub>1</sub>) and N(d<sub>2</sub>):

$$N(d_1) = 0.73401$$
  
 $N(d_2) = 0.53079$ 

$$V = P[N(d_1)] - Xe^{-r_{RF}t}[N(d_2)] = 8.6(0.73401) - 8e^{-0.06(2)}(0.53079) = \$2.55 \ million$$

The total value is the value of the original project (from part a) and the value of the growth option:

Total value = 
$$$3.38 + $2.55 = $5.93$$
 million

# CHAPTER 26

ST-1 a. Value of unleveraged firm,  $V_U = EBIT(1 - T)/r_{sU}$ :

$$\begin{array}{lcl} \$12 & = & \$2(1{\text -}0.4)r_{sU} \\ \$12 & = & \$1.2/r_{sU} \\ r_{sU} & = & \$1.2/\$12 = \$10.0\% \end{array}$$

Therefore,  $r_{sU} = WACC = 10.0\%$ .

b. Value of leveraged firm according to MM mode with taxes:

$$V_L = V_U + TD$$

As shown in the following table, value increases continuously with debt, and the optimal capital structure consists of 100% debt. Note: The table is not necessary to answer this question, but the data (in millions of dollars) are necessary for part c of the problem.

DEBT, D	$\mathbf{V}_{\mathbf{U}}$	TD	$V_L = V_U + TD$
\$ 0.0	\$12.0	\$0.0	\$12.0
2.5	12.0	1.0	13.0
5.0	12.0	2.0	14.0
7.5	12.0	3.0	15.0
10.0	12.0	4.0	16.0
12.5	12.0	5.0	17.0
15.0	12.0	6.0	18.0
20.0	12.0	8.0	20.0

c. With financial distress costs included in the analysis, the value of the leveraged firm is now

$$V_L = V_U + TD - PC$$

where

 $V_U + TD = Value$  according to MM after-tax model.

P = Probability of financial distress.

C = Present value of distress costs.

D	$V_U + TD$	P	PC = (P)\$8	$V_L = V_U + TD - PC$
\$ 0.0	\$12.0	0.0000	\$0.00	\$12.0
2.5	13.0	0.0000	0.00	13.0
5.0	14.0	0.0125	0.10	13.9
7.5	15.0	0.0250	0.20	14.8
10.0	16.0	0.0625	0.50	15.5
12.5	17.0	0.1250	1.00	16.0
15.0	18.0	0.3125	2.50	15.5
20.0	20.0	0.7500	6.00	14.0

Note: All dollar amounts are in millions.

Optimal debt level: D = \$12.5 million. Maximum value of firm: V = \$16.0 million.

Optimal debt/value ratio: D/V = 12.5/16 = 78%.

d. The value of the firm versus debt value with and without financial distress costs is plotted next (millions of dollars), where

 $V_L = Value$  without financial distress costs.

 $V_B = Value \ with \ financial \ distress \ costs.$ 

